

MAC 1105 Formulas

Slope of a line	$m = \frac{y_2 - y_1}{x_2 - x_1}$
Slope-intercept form	$y = mx + b,$
Point-slope form	$y - y_1 = m(x - x_1)$ or $y = m(x - x_1) + y_1$
Slope of parallel lines	$m_1 = m_2$
Slope of perpendicular lines	$m_2 = \frac{-1}{m_1}$ or opposite reciprocal
Special lines	$y = b;$ horizontal line, $x = a;$ vertical line
Quadratic formula	Given $ax^2 + bx + c = 0;$ $x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$
Vertex (max or min)	$\left(\frac{-b}{2a}, f\left(\frac{-b}{2a}\right)\right)$
x-intercept	Let $y = 0;$ (a, 0)
y-intercept	Let $x = 0;$ (0, b)

Money and Depreciation

$$A = P(1 + r/n)^{nt}$$

$$A = Pe^{rt}, \text{ use when continuous}$$

$$V = a(b)^t; b = 1 \pm r$$

$$\text{Double time} = \frac{\ln(2)}{r}$$

$$\text{half-life} = \frac{\ln(.5)}{r}$$

Solving Absolute Value Equations

$$|a+b| > c \rightarrow (a+b) > c \text{ or } (a+b) < -c$$

$$|a+b| < c \rightarrow (a+b) < c \text{ and } (a+b) > -c \text{ or}$$

$$|a+b| < c \rightarrow -c < (a+b) < c$$

Translation rules

$y = f(x + a)$	a units to the left
$y = f(x - a)$	a units to the right
$y = f(x) + a$	a units up
$y = f(x) - a$	a units down
$y = -f(x)$	Reflected over the x axis
$y = f(-x)$	Reflected over the y axis
Is $f(x) = f(-x)$	Symmetric to the y axis
Is $f(x) = -f(x)$	Symmetric to the x axis
Is $f(x) = -f(-x)$	Symmetric to the origin
$y = cf(x)$	$c > 1:$ stretch vertically, $0 < c < 1:$ compress vertically

Logarithm rules

$\log_a mn = \log_a m + \log_a n$
$\log_a \frac{m}{n} = \log_a m - \log_a n$
$\log_a m^p = p \log_a m$
$\log_a x = y \leftrightarrow a^y = x$
$\log_a m = \frac{\log m}{\log a} = \frac{\ln m}{\ln a}$
$\ln e^x = x \text{ and } e^{\ln x} = x$
$\log_a a^x = x \text{ and } a^{\log_a x} = x$
if $a^x = a^y; a \neq 0,$ then $x = y$
$\log_a m = \log_a n; m, n > 0,$ then $m = n$
$\log_a a = 1 \text{ and } \ln_e e = 1 \text{ and } \log_a 1 = 0$

Exponent Rules

$m^a m^b = m^{a+b}$	$(m^a)^b = m^{ab}$
$\frac{m^a}{m^b} = m^{a-b}$	$m^{-a} = \frac{1}{m^a}$
$m^0 = 1$	$\sqrt[b]{m^a} = m^{\frac{a}{b}}$
n even, $\sqrt[n]{a^n} = a $	n odd, $\sqrt[n]{a^n} = a$
$i = \sqrt{-1}, i^2 = -1$	$\sqrt{-m} = i\sqrt{m}$

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